



**GHENT
UNIVERSITY**

SIMULATING N-BODY SYSTEMS

Simon Donné, November 9th 2016

OVERVIEW OF THE PRESENTATION

Problems and solutions

Full-on simulation

Attraction fields

Octree approximation

Out of memory problems

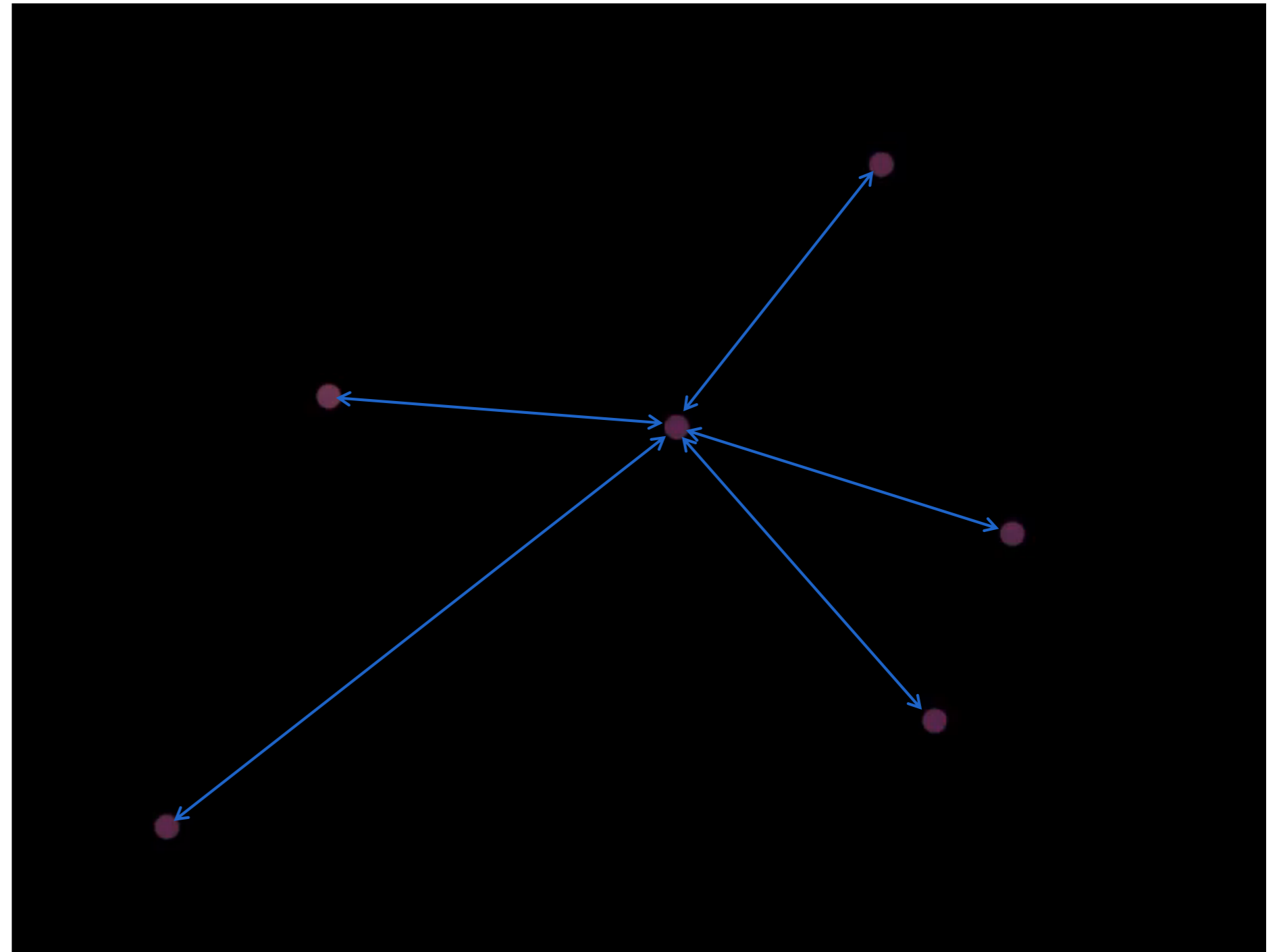
PROBLEMS AND SOLUTIONS

Every particle influences every other particle

6 particles: 15 interactions

81'920 particles: 3'355'402'240 interactions

Calculating them all is a lot of work: $O(n^2)$!



PROBLEMS AND SOLUTIONS

All implementation is done using Quasar

An in-house developed programming language

GPU programming through automatic code generation

Automatic optimization of kernel parameters

Perfect for prototyping!

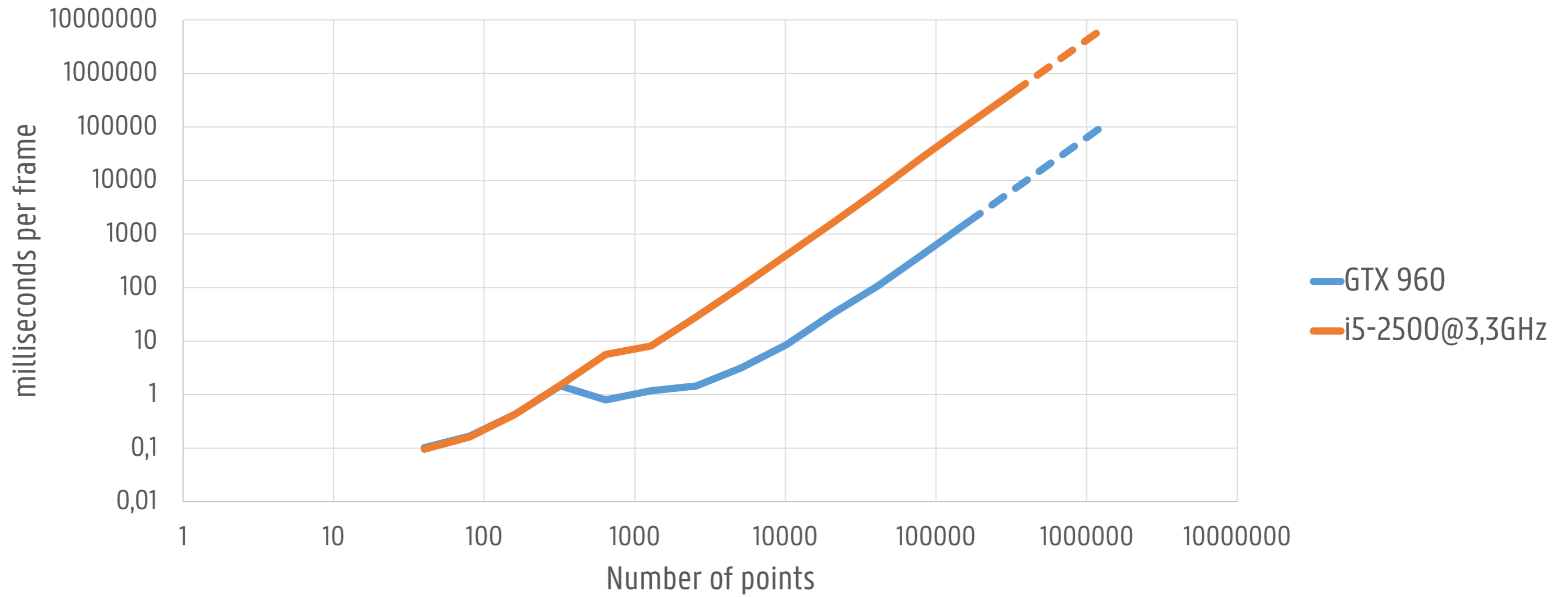
Incremental implementation times given for all methods

FULL-ON SIMULATION

Full implementation time: 3 hours

The ground-truth approach

Calculate all $n(n-1)$ attractions



ATTRACTION FIELDS

Each point throws an attraction field in the space around it

We approximate these attraction fields

ATTRACTION FIELDS

Incremental implementation time: 0,5 hours

Attempt 1: DxDxD voxel cube

For each voxel, calculate the effects of all points on it

Then each point simply looks up its location in the cube

Calculating the field: $O(nD^3)$

TOO SLOW

Field lookup: $O(n)$

ATTRACTION FIELDS

Incremental implementation time: 1,5 hours

Attempt 2: a hierarchy of voxel cubes (height h , subdivision D)

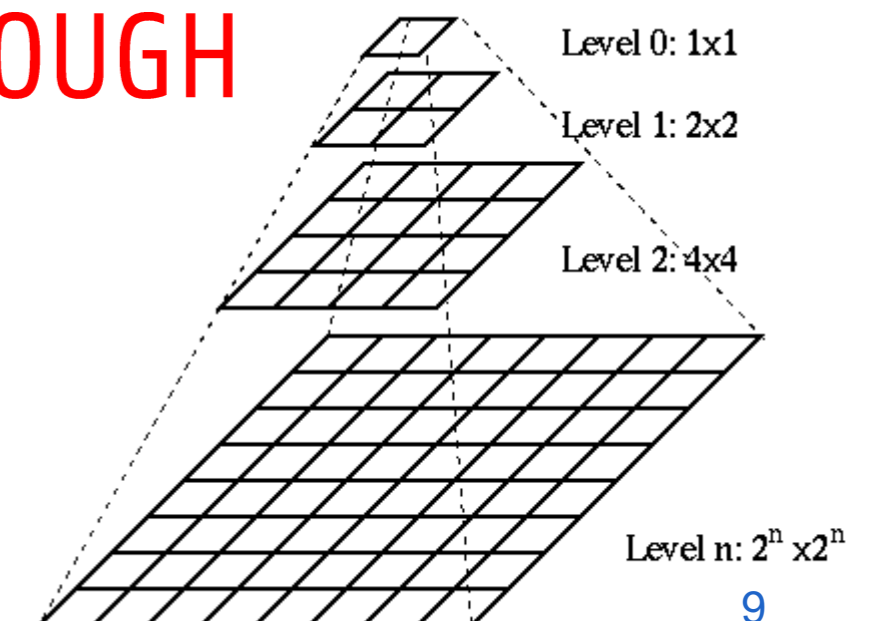
we use $h=9$, $D=2$

At each level, we calculate the exerted attraction on all voxels we are not in, and continue recursively into the voxel we *are* in.

Calculating the field: $O(h(D^3-1)n)$

Calculating the field: $O(hn)$

NOT FINE ENOUGH

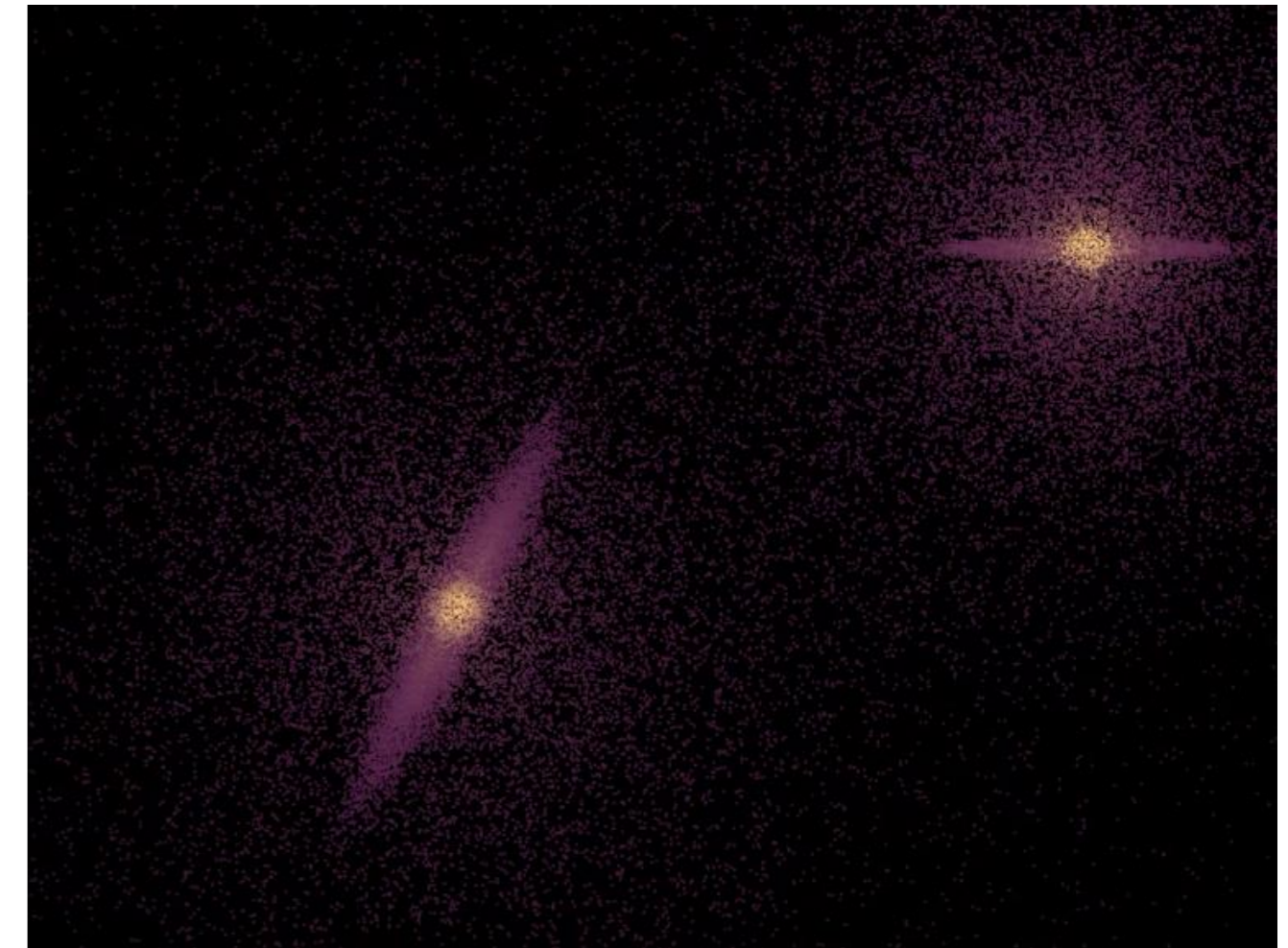
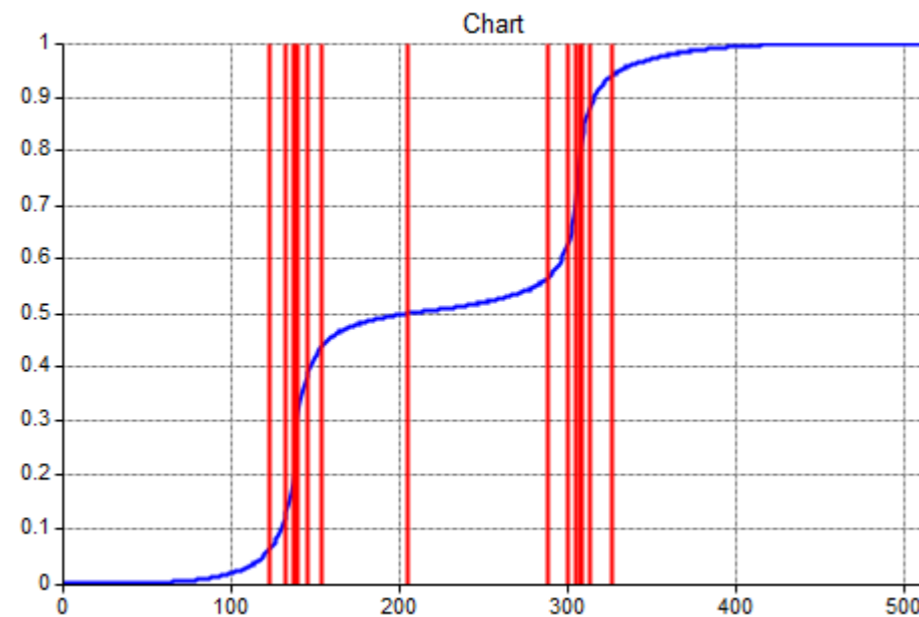
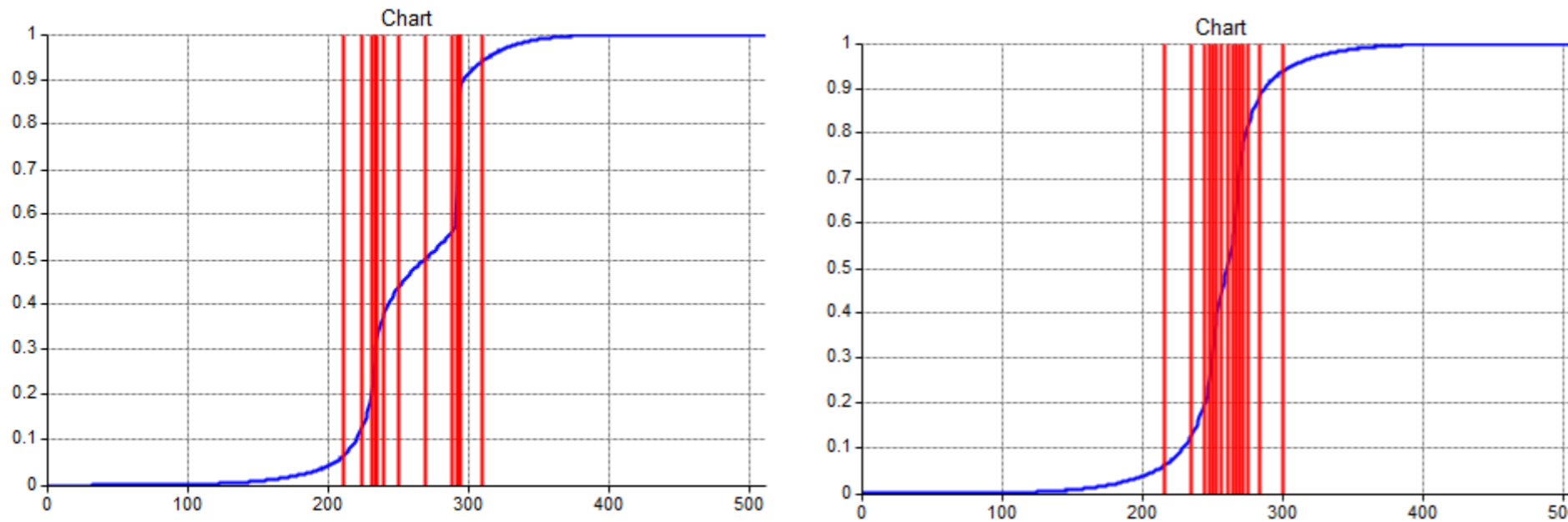


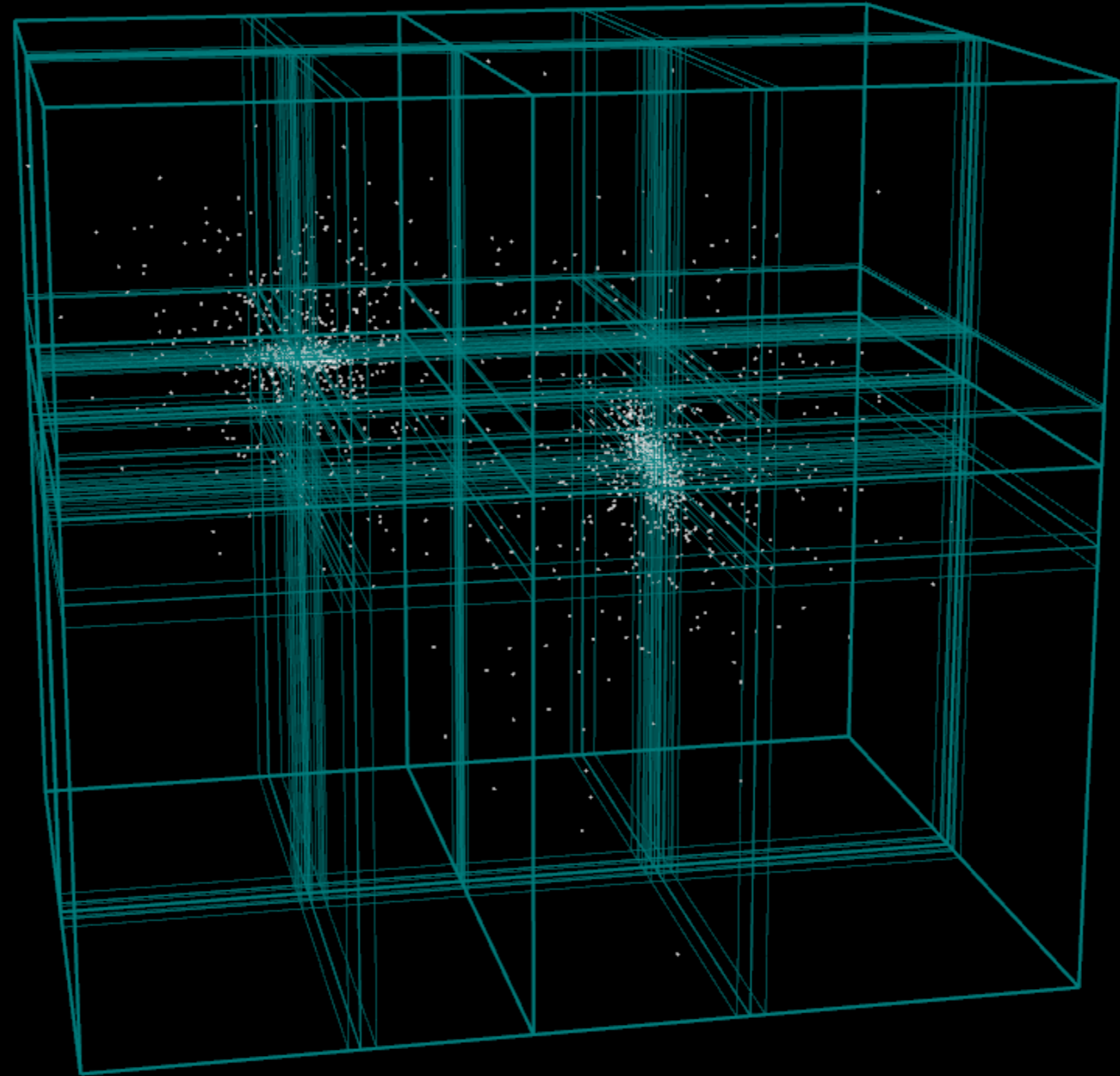
ATTRACTION FIELDS

Incremental implementation time: 1,5 hours

Attempt 2: a hierarchy of nonuniform voxel cubes

The voxel cubes are no longer uniform





ATTRACTION FIELDS

Incremental implementation time: 3,5 hours

Attempt 3: a hierarchy of nonuniform voxel cubes

The voxel cubes are no longer uniform

Nice properties:

Calculating the subdivisions: $O(nD^h)$

Calculating the field: $O(h(D^3-1)n)$

Calculating the field: $O(hn)$

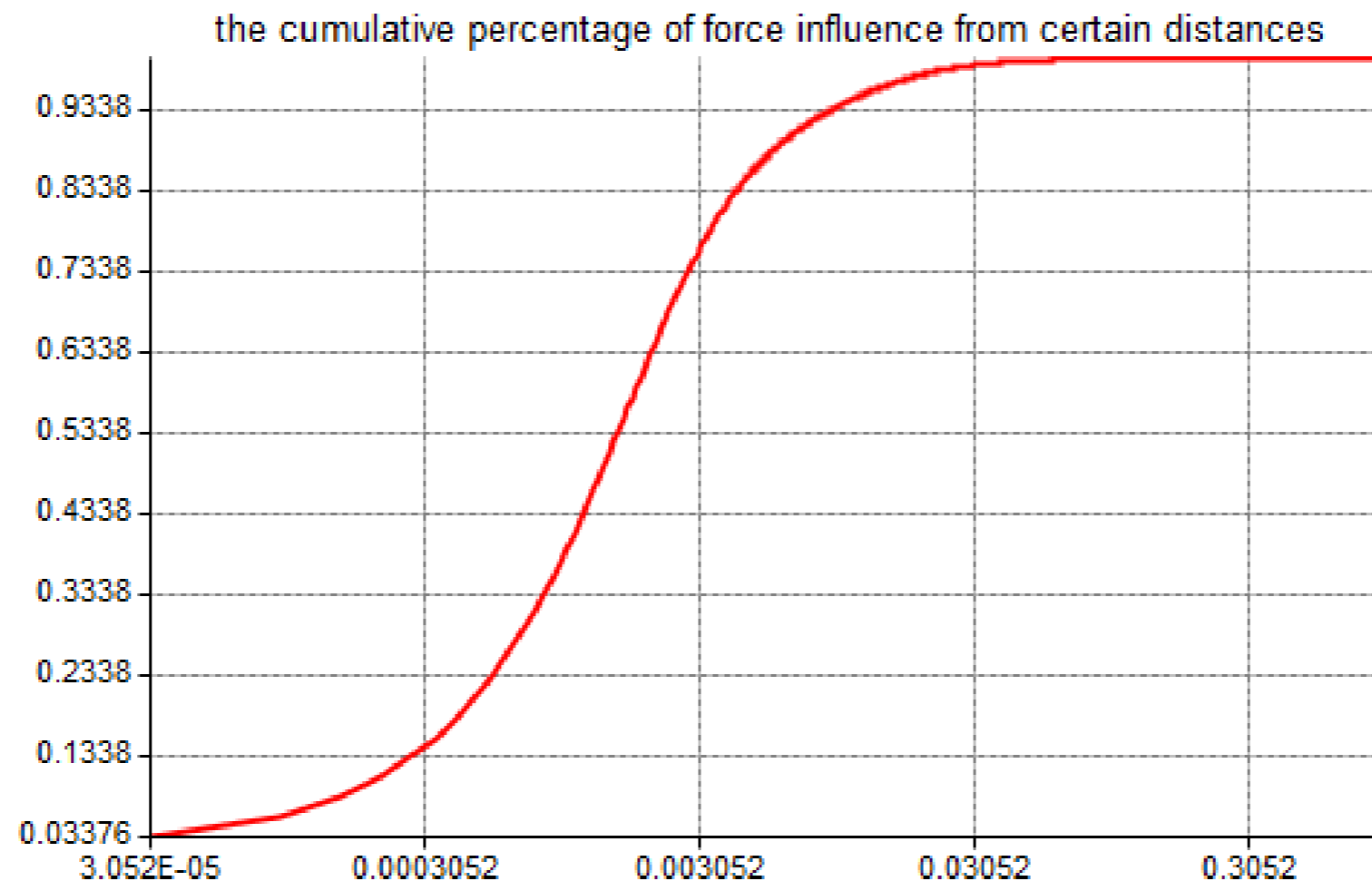
STILL NOT FINE ENOUGH

OCTREE APPROXIMATION

The attraction field method failed

Gravitational attraction is ruled by close objects

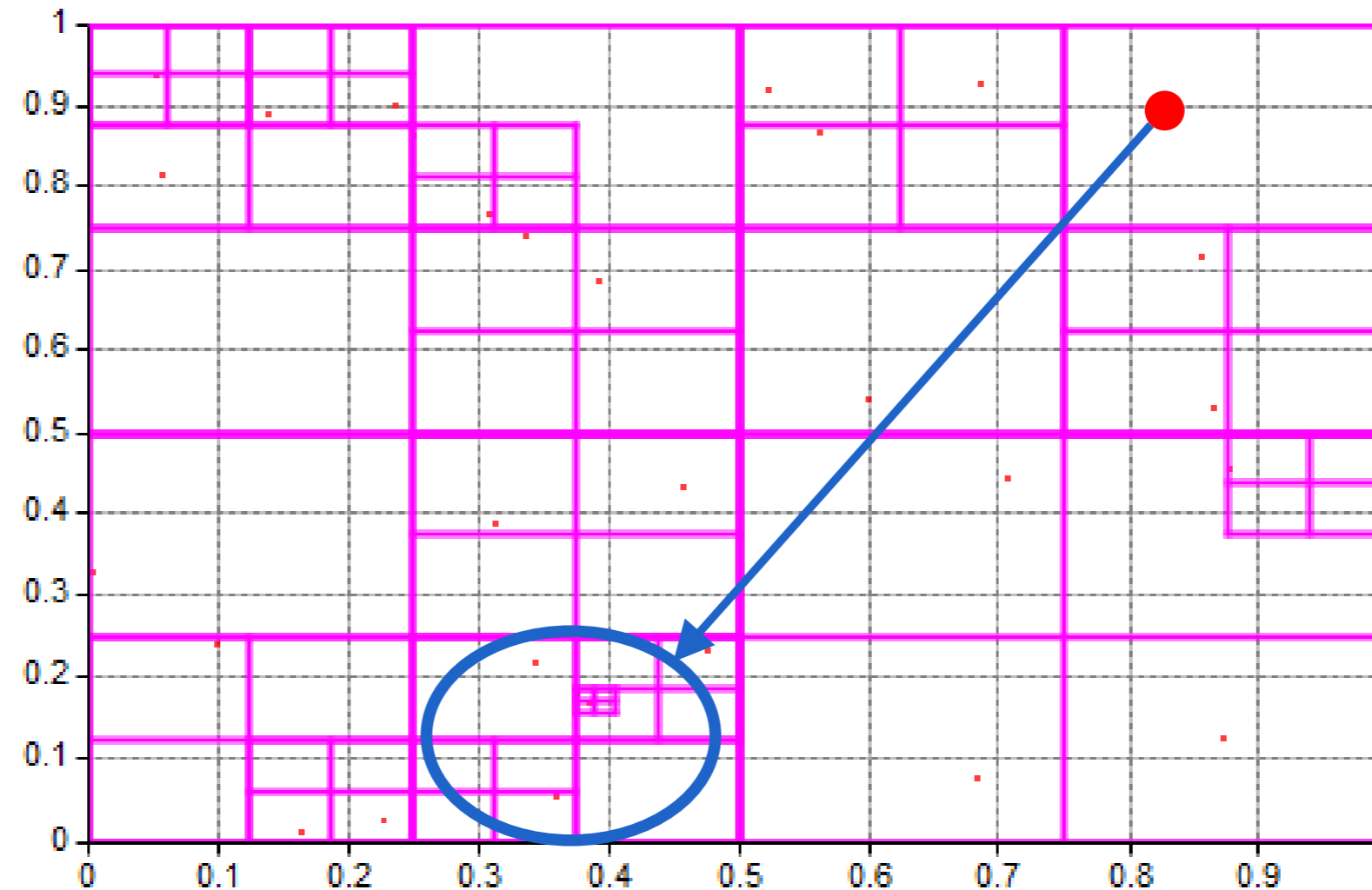
Even though the milky way dataset has this distribution:



OCTREE APPROXIMATION

Approximate large far-away clusters as a single point

Using oct-trees



The oct-tree implementation is based on

“Parallel construction of quadtrees and quality triangulations”

1. Interleave the bits of the fixed-point float coordinates
2. Sort the list



Octant 4

The oct-tree implementation is based on

“Parallel construction of quadtrees and quality triangulations”

3. From this list, the tree can be built in a straightforward manner

Total complexity: $O(n \log(n))$

4. Nice GPU optimization step

We have the points ordered spatially

i.e. points following the same path through the tree

Use these for selecting kernel blocks

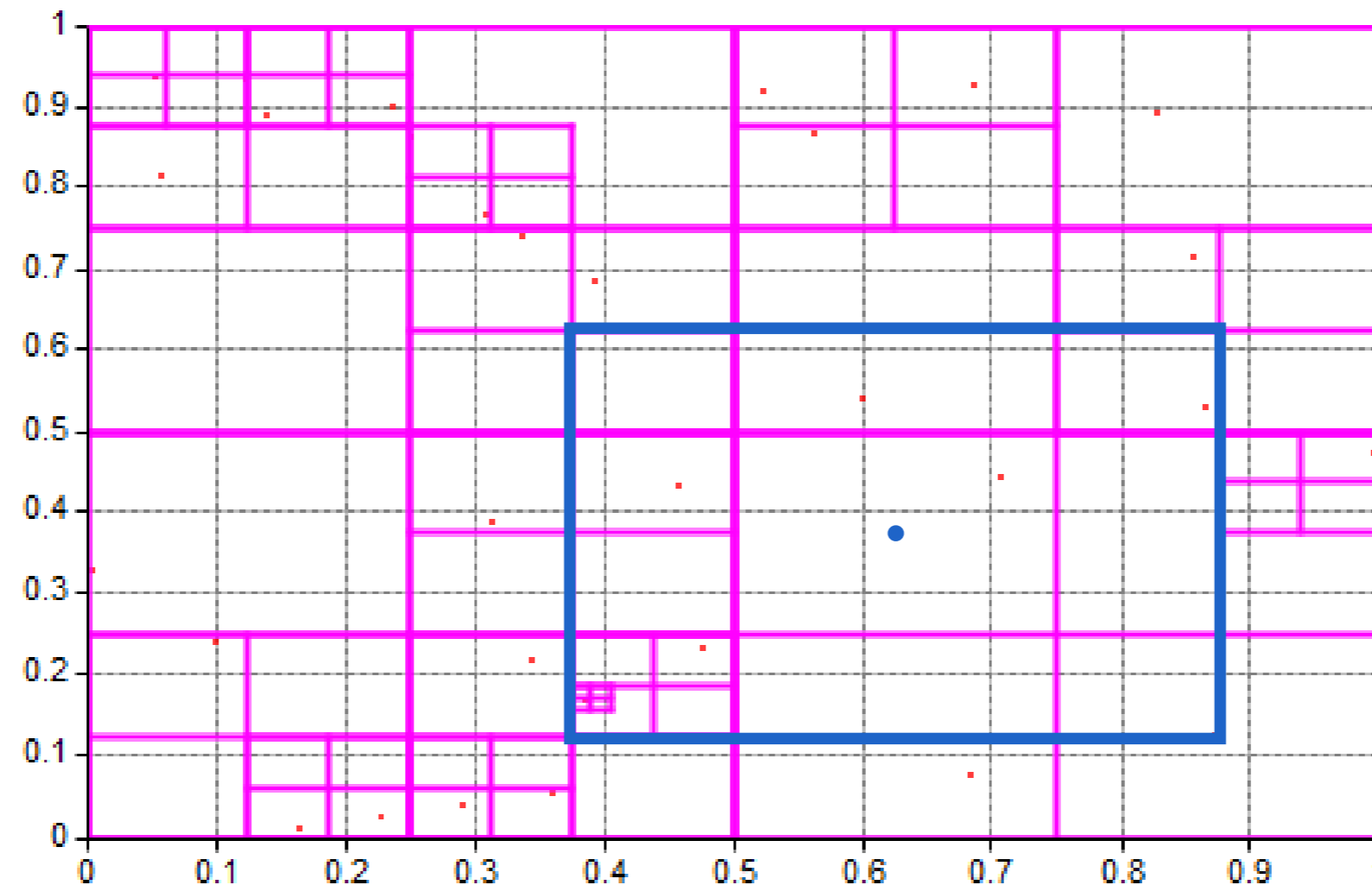
↔ arbitrary ordering from original file read

OCTREE APPROXIMATION

Incremental implementation time: 5 hours

Accuracy: when do we approximate tree nodes as a single cluster?

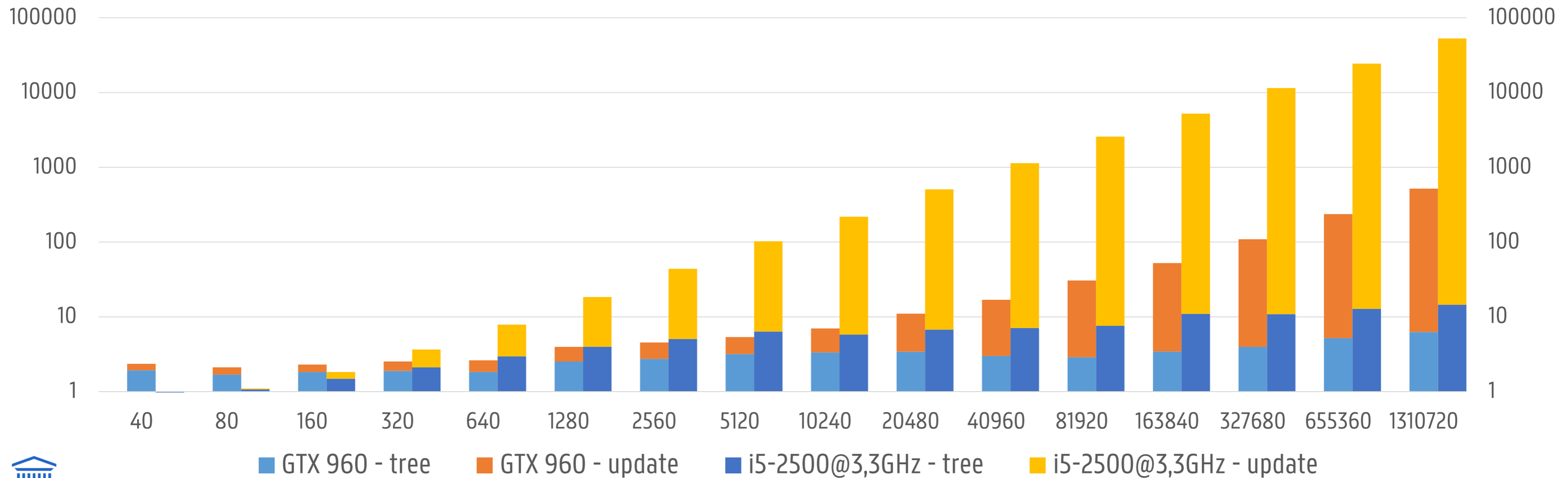
Heuristic rule: point is not in the twice-as-wide cube



OCTREE APPROXIMATION

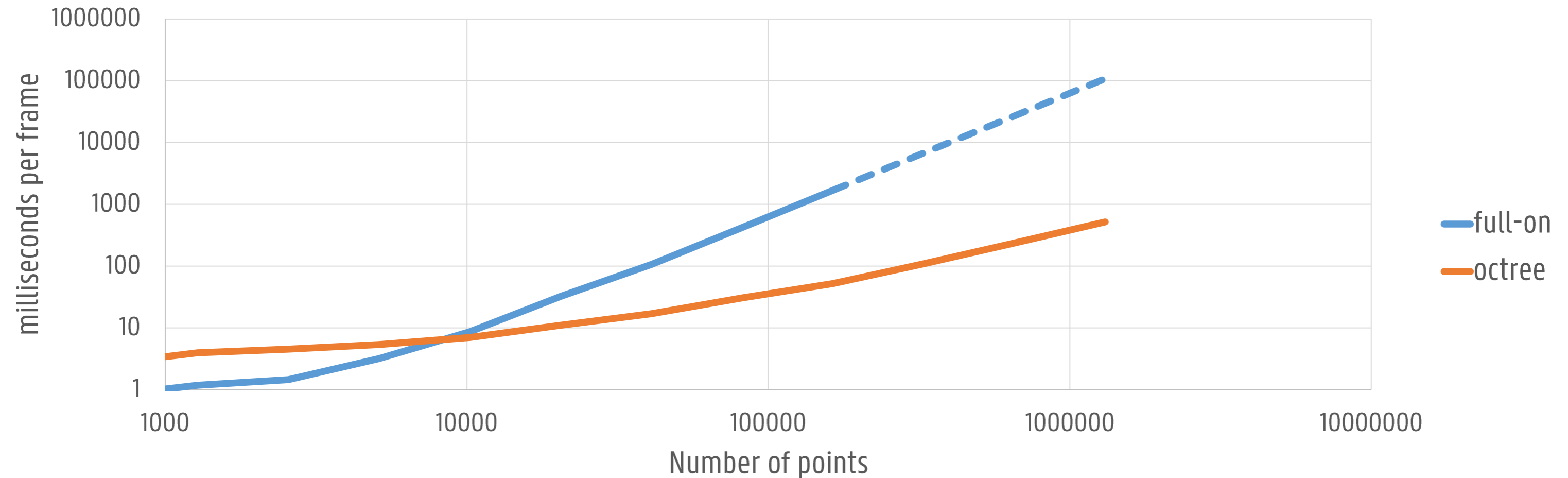
The resulting approach is translated well to GPU

Milliseconds per frame vs. number of points



OCTREE APPROXIMATION

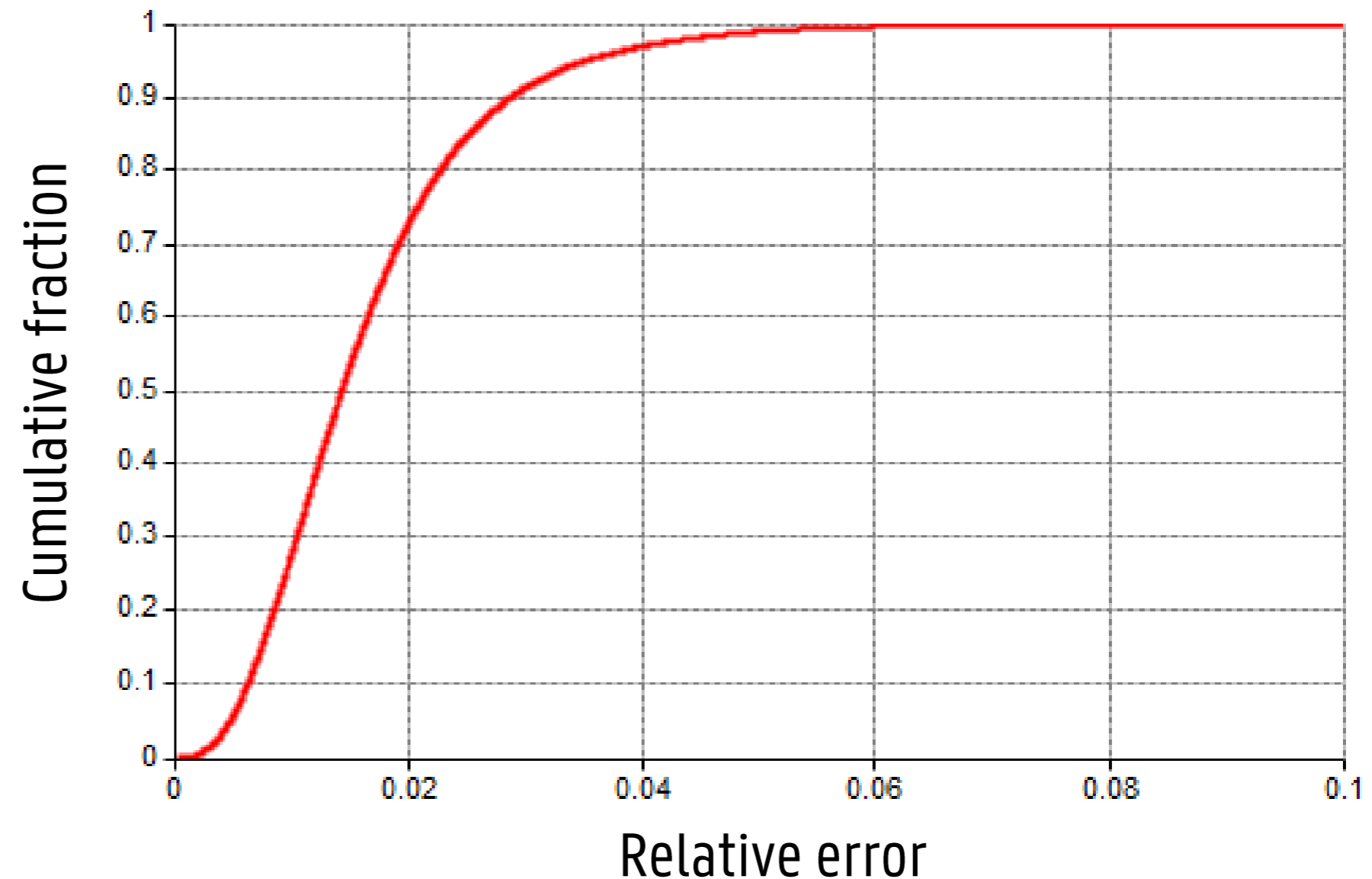
Much faster than full-on calculations!



OCTREE APPROXIMATION

The resulting simulation is close to the full-on simulation
For the Milky Way/Andromeda cluster collision

mean error ~1,5%
stddev error ~1%



OUT OF MEMORY PROBLEMS

Two possible problems:

- Memory constraint
- CUDA kernel runtime (max 5s)

SPLIT UP DATASETS INTO SEGMENTS

Or, a positive reason:

- Multiple GPUs available

OUT OF MEMORY PROBLEMS

Forces are additive, so:

- 1) Make a separate tree for each segment of points
one kernel per segment
- 2) Calculate the attractions of each tree on each segment
one kernel per segment per tree